



Stellar radial migration as a subdiffusive process

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Simulations of Milky-Way like galaxies suggest that stellar radial migration does not happen continuously, but in episodes. However, in observational works migration is typically treated as a diffusive process. We use a new suite of cosmological Milky-Way-like simulations, NIHAO-UCD, to show that radial migration should not be approximated as one-dimensional diffusion along the radial axis of a galaxy. In particular we show that 1.) the net migration shows characteristic quasi-periodic oscillations, 2.) the power spectrum of radial migration is significantly different from white noise, and 3.) the migration efficiency depends both on age and on the birth position of a star, with a power-law coefficient around $1/4$. We conclude that on Galactic evolution timescales radial migration should rather be described as a subdiffusive than as a diffusive process.



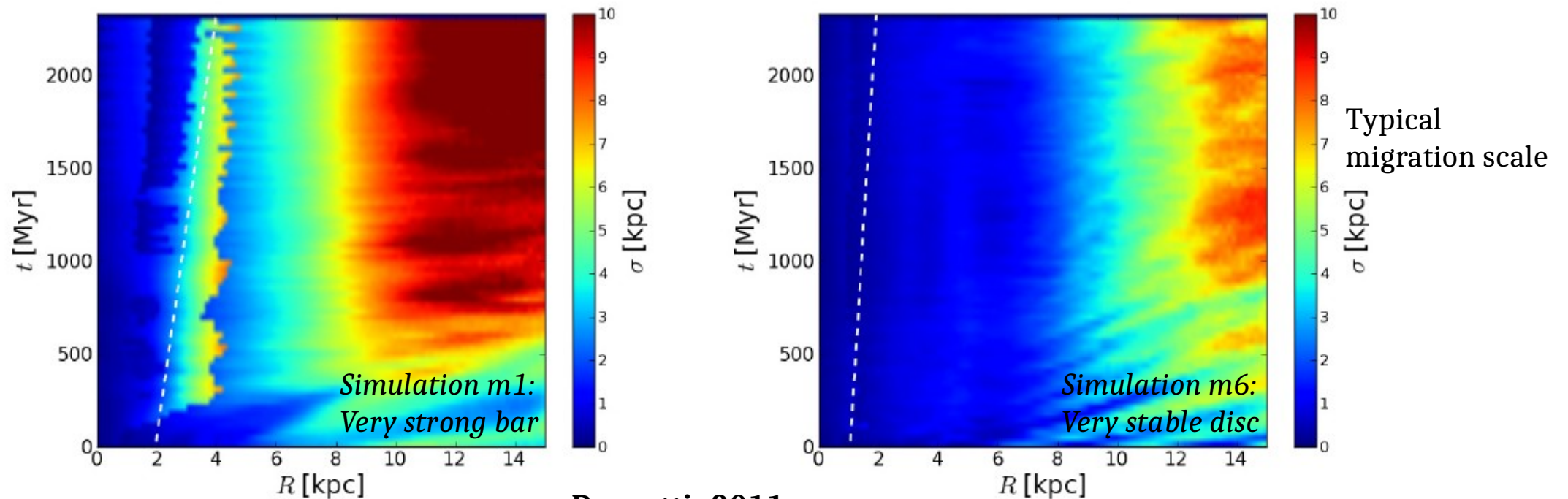
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Problem: how do we treat stellar radial migration correctly?

Sellwood & Binney 2002: Radial mixing = blurring + churning. To 1st approximation: churning=diffusion
Kubryk+2015, Frankel+2018, Sharma+2020: Churning modelled as diffusion in R
Frankel+2019, 2020: Churning modelled as diffusion in action space

Brunetti+2011: you can locally assume diffusion, but this will only be valid over ~ 1 rotation...



Brunetti+2011

Migration in the NIHAO-UHD simulations

Simulations:

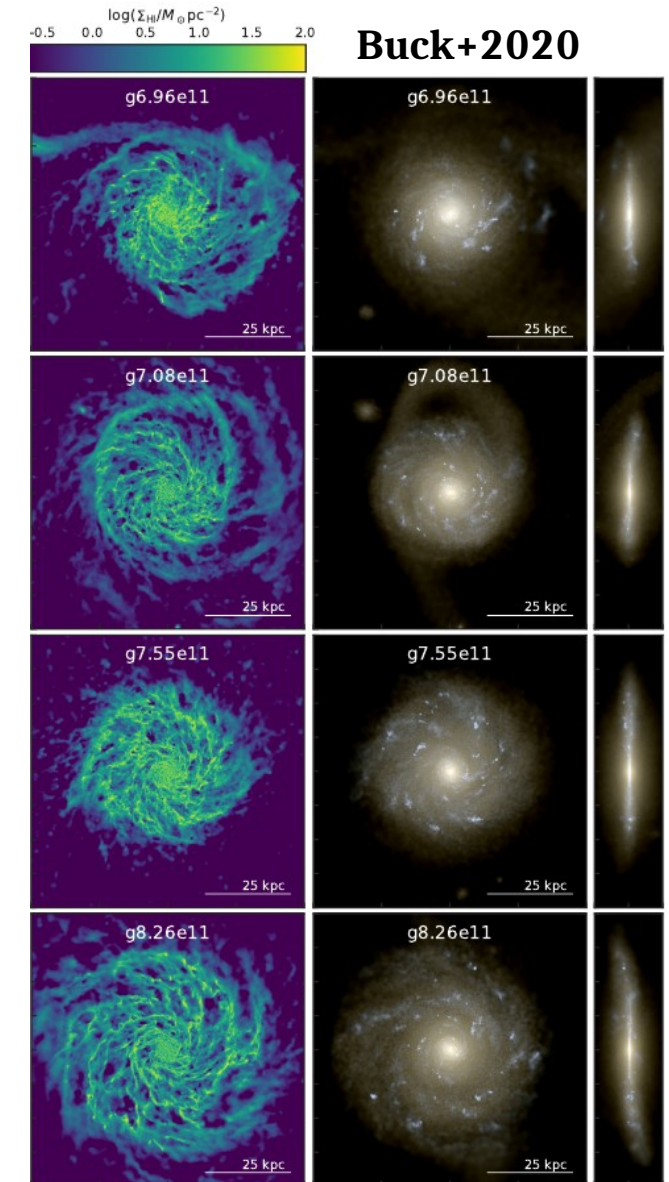
- 5 cosmo zoom-in SPH discs that bracket the MW mass (Buck et al. 2020)
- Stellar chemo-dynamics studied in more detail in Buck 2020 (explaining the α/Fe disc bimodality present in the MW)

Data used:

- $z=0$ snapshots
- birth radii for each particle
- focussing on the stellar disc component born in-situ ($|Z_{\text{birth}}| < 2$, $|Z| < 3$, $R < 20$, $R_{\text{birth}} < 20$)
- to study migration we look at the distribution $\{R, R_{\text{birth}}, \text{age}\}$ in various projections. This relies on the following **assumptions** (which might also be broken!):

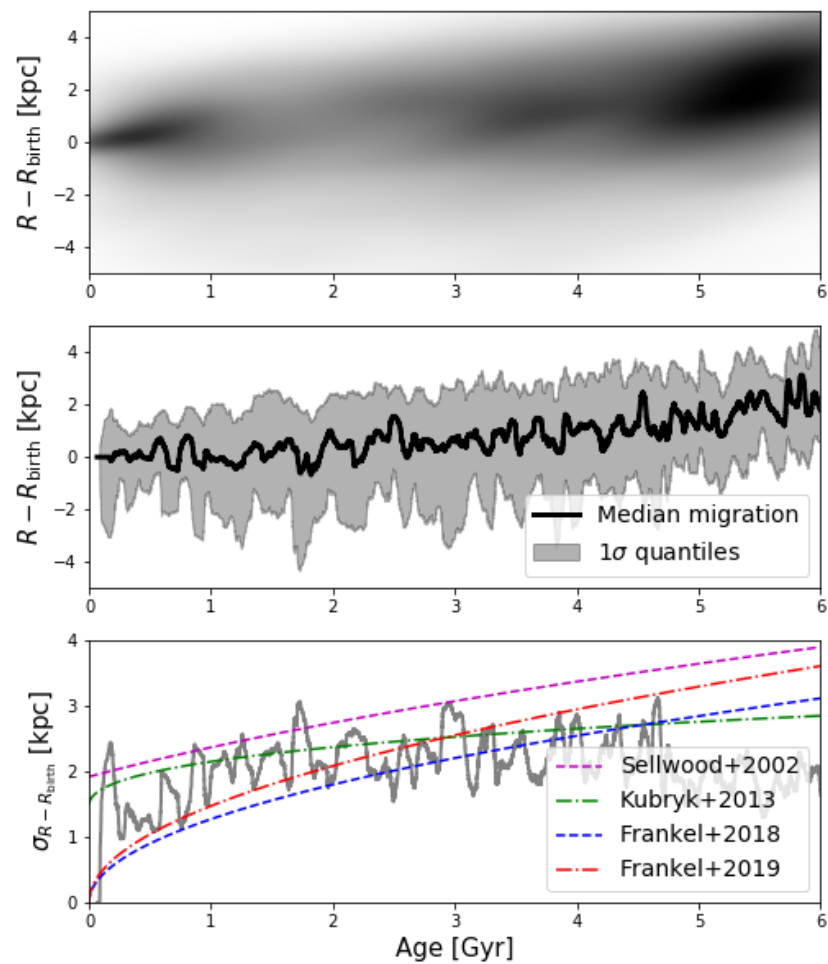
* Time reversibility: $\text{age} == -\text{time}$

* Ergodicity: Average over all particles at 1 age in an initial volume = average of all trajectories that are in volume at time $t=t_0$



(Preliminary) Results: Signs of subdiffusive behaviour

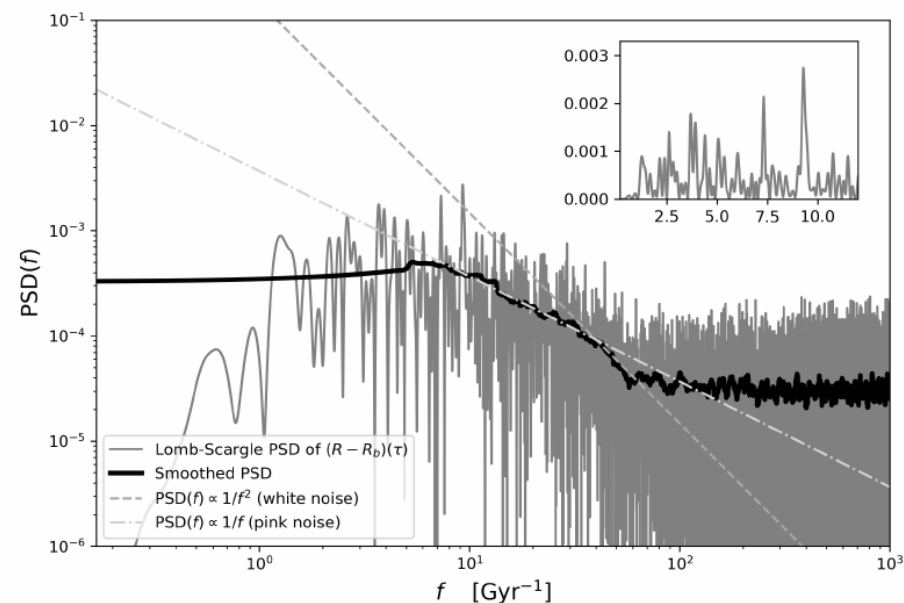
Radial mixing in NIHAO-UHD g7.55e11
(7.5 kpc < R_{birth} < 8.5 kpc)



We study the $R - R_{\text{birth}}$ distribution as a function of age, $p(R - R_{\text{birth}} | \text{age})$ in bins of R_{birth} :

- we look at the median trend + the dispersion around the median
- both the median trend & the dispersion show conspicuous wiggles
- the dispersion does not seem to follow a diffusion law

Power spectrum of radial migration in g7.55e11 (7 kpc < R_{birth} < 9 kpc)



The power spectrum of $p(R - R_{\text{birth}} | \text{age})$ gives clues about the underlying dynamics:

- If migration = diffusion, then we would expect a white-noise-like spectrum $\text{PSD}(f) \sim 1/f^2$. However, we see some interesting low-frequency peaks and a pink-noise-like ($\sim 1/f$) behaviour up to intermediate frequencies.

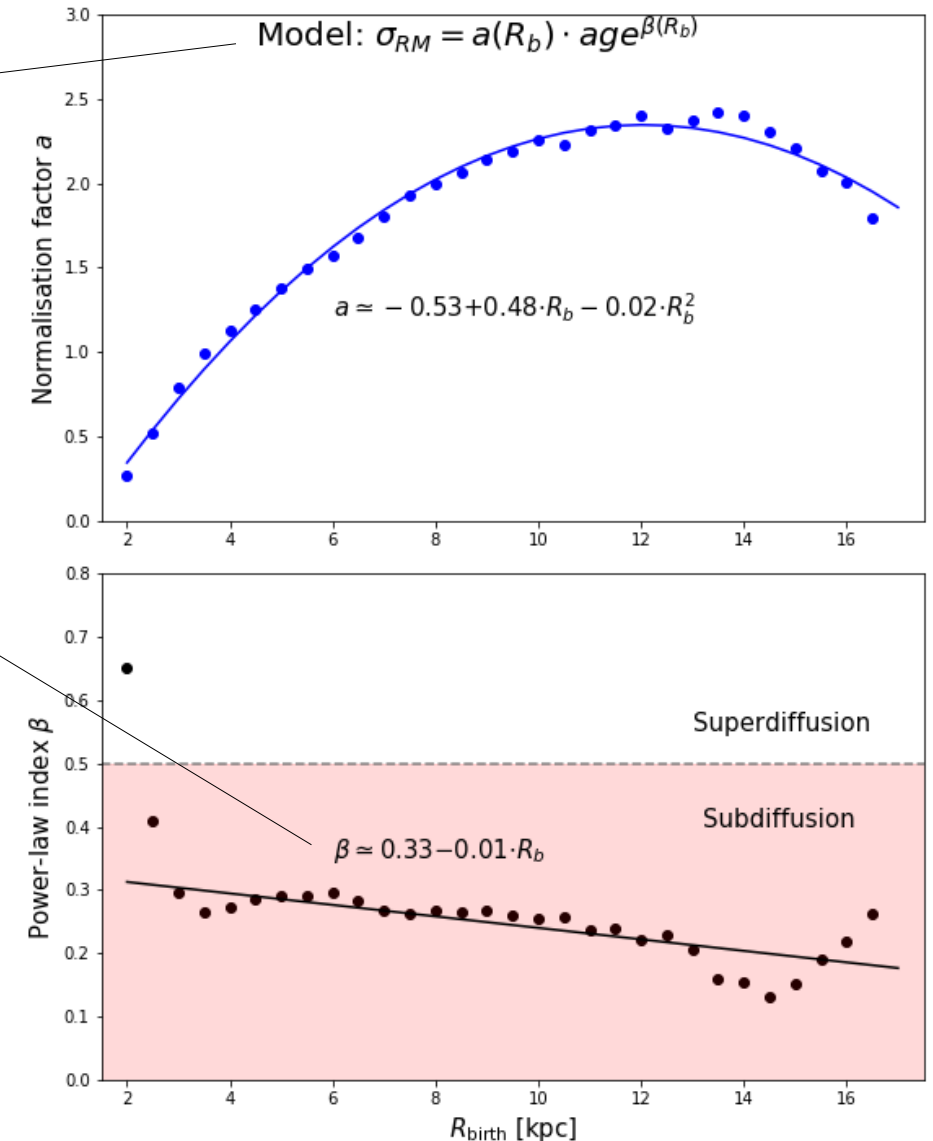
(Preliminary) Results: Signs of subdiffusive behaviour

Migration efficiency can be modelled well as a product of a term depending on R_{birth} and an age-dependent power-law term.

For all but the innermost R_{birth} bin, the dispersion dependence on age has a power-law index ~ 0.2 - 0.3 (similar values for all 5 NIHAO-UHD disc galaxies), which indicates subdiffusive behaviour.

This is a normal behaviour in complex dynamical systems (especially in non-equilibrium).

(e.g. Bak, Tang & Wiesenfeld 1987)



Implications

1. When fitting Milky Way data with semi-analytic models (e.g. Frankel+2020), we should **use more flexible descriptions** for radial migration (that can account for the observed subdiffusive behaviour).
2. The importance of this **effect on star-formation history** inferences (e.g. Mor+2019, Isern 2019, Ruiz-Lara+2020) could potentially be sizeable.

Future

1. We need to verify that the behaviour is **not a peculiarity of the NIHAO-UHD simulations**, but a universal feature in Milky-Way simulations.
2. The analysis will be extended to **action space**.
3. Subdiffusive behaviour usually implies **broken ergodicity**. This can be verified by comparing our analysis to a similar one studying the particle trajectories over all snapshot.